## We Claim:

- 1. A method for authenticating a data set between a proving unit and a verifying unit, which comprises the steps of:
- a) communicating the data set from one of the proving and verifying units to a respective other of the proving and verifying units such that the data set is in an unencrypted form to both the proving and verifying units after completing the communicating step;
- b) generating at least one data element in the verifying unit;
- c) using the verifying unit to encrypt the data element in a first cryptographic encryption method using a public key of the proving unit resulting in at least one encrypted data element, and the public key is known to the verifying unit;
- d) communicating the encrypted data element from the verifying unit to the proving unit;
- e) using the proving unit to decrypt the encrypted data element in a first decryption method, assigned to the first encryption method, using a private key known only to the proving unit;

- f) using the proving unit to calculate, from the data set to be authenticated, in a second cryptographic method, an authenticator dependent on the data element;
- g) communicating the authenticator from the proving unit to the verifying unit;
- h) using the verifying unit to check the authenticator with an aid of an authentication checking algorithm, assigned to the second cryptographic method using the data element and the data set; and
- i) accepting the data set as communicated by the proving unit to the verifying unit in dependence on a result of the checking step.
- 2. The method according to claim 1, which further comprises during the step a), using the proving unit to communicate the data set in unencrypted form to the verifying unit.
- 3. The method according to claim 1, which further comprises using the verifying unit to generate the data set as a random element and subsequently, in the step a), communicating the data set to the proving unit.

4. The method according to claim 1, which further comprises during the step h):

forming the authentication checking algorithm to be substantially identical to the second cryptographic method for authenticator generation;

applying the authentication checking algorithm by the verifying unit to the data element and the data set for forming a reference authenticator; and

comparing the reference authenticator with the authenticator.

5. The method according to claim 1, which further comprises during the step h):

forming the authentication checking algorithm with a decryption method corresponding to the second cryptographic method for generating the authenticator for an associated encryption method;

applying the authentication checking algorithm by the verifying unit to the authenticator by decryption for forming a reference data element and a reference data set; and

comparing the reference data element and the reference data set with the data element and the data set.

6. The method according to claim 1, which further comprises:

repeating steps b), c), d) and e) for generating at least one further data element before performing the step f); and

using the proving unit to encrypt the data set to be authenticated in step f) in a manner dependent on the data element and the further data element to form the authenticator.

- 7. The method according to claim 1, which further comprises carrying out the first cryptographic encryption method and the first decryption method assigned thereto using discrete exponentiation in a semigroup.
- 8. The method according to claim 7, which further comprises carrying out the first cryptographic encryption method and the first decryption method assigned thereto using an algorithm based on elliptical curves.
- 9. The method according to claim 7, which further comprises performing the first cryptographic encryption method with the steps of:

using the verifying unit to generate a number  $t \in T$ , where T is a subrange of integers;

using the verifying unit to calculate element  $h^{f(t)} \in H$ , where  $f: T \to T'$  is a mapping into a subrange T' of the integers, which is not necessarily different from T, H represents a multiplicatively written semigroup generated by element h, with a discrete exponentiation of a base h as a one-way function in the semigroup H;

using the verifying unit to calculate from the public key,  $k_{pub}$  =  $h^{f(d)} \in H$ , element  $\pi(k_{pub}{}^{f(t)}) \in G$ , where  $\pi: H \to G$  specifies a mapping of the semigroup H into a group G,  $d \equiv k_{priv} \in T$  is the private key which is accessible only to the proving unit, and a mapping  $t \to h^{f(t)} \to \pi(h^{f(t)})$  from the subrange of the integers T to the group G represents a one-way function; and

using the verifying unit to encrypt the data element, z, by a combination with respect to the encrypted data element, z'=z  $\circ \pi(k_{pub}{}^{f(t)}) \in G.$ 

10. The method according to claim 9, which further comprises during the step d), in addition to the encrypted data element,

using the verifying unit to communicate the element  $h^{f(t)} \in H$  to the proving unit.

11. The method according to claim 10, which further comprises performing the first cryptographic decryption method by the steps of:

using the proving unit to calculate the element  $k_{pub}^{f(t)} \in H$  using function f, the element  $h^{f(t)} \in H$  and the private key d known only to the proving unit;

using the proving unit to calculate an inverse element  $\pi'(k_{pub}{}^{f(t)}) \,\in\, G \text{ with respect to element } \pi(k_{pub}{}^{f(t)}) \,\in\, G; \text{ and }$ 

using the proving unit to decrypt the encrypted data element by a combination of the encrypted data element with inverse element:  $z=z'\circ\pi'(k_{pub}{}^{f(t)})$ , where the first cryptographic decryption method is based on the same mappings f,  $\pi$  and the same combination  $\circ$  as the first cryptographic encryption method.

12. The method according to claim 11, which further comprises performing the second cryptographic method with the steps of:

using the proving unit to calculate, from the at least one unencrypted data element z, an element  $g_2 = \pi_1(z) \in G_1$  and an element  $g_2 = \pi_2(z) \in G_2$ , where  $G_{-1}$  and  $G_2$  represent groups where  $G_1 \subset G_2$  and  $\pi_1 : G \to G_1$  and  $\pi_2 : G \to G_2$  represent functions which map elements of the group  $G_1$  onto the groups  $G_1$  or  $G_2$ ;

using the proving unit to transform the data set to be authenticated m, to form an element  $g'=(g_1*m)$  with a group combination \* in  $G_1$ ; and

using the proving unit to calculate the authenticator D, by D = inj(g') •  $g_2$  with the group combination • in  $G_2$ , where the mapping inj :  $G_1 \rightarrow G_2$  maps elements from  $G_1$  injectively into  $G_2$ .

13. The method according to claim 1, which further comprises performing the following steps before performing step b):

using the proving unit to communicate the public key with a certificate of a trust center;

using the verifying unit to check a validity of the public key of the proving unit using a certification method; and

using the verifying unit to continue the communication with the proving unit in a manner dependent on a result of the check.

14. The method according to claim 1, which further comprises:

forming the proving unit as an integrated circuit on a smart card; and

forming the verifying unit as a smart card terminal.

- 15. The method according to claim 1, which further comprises forming the proving unit as an integrated circuit in an identification/authentication token which is fixedly connected to a non-localized object.
- 16. The method according to claim 14, which further comprises performing the communication between the proving unit and the verifying unit contactlessly.
- 17. The method according to claim 8, which further comprises performing the first cryptographic encryption method with the steps of:

using the verifying unit to generate a number  $t \in T$ , where T is a subrange of integers;

using the verifying unit to calculate element  $h^{f(t)} \in H$ , where  $f: T \to T'$  is a mapping into a subrange T' of the integers, which is not necessarily different from T, H represents a multiplicatively written semigroup generated by element h, with a discrete exponentiation of a base h as one-way function in the semigroup H;

using the verifying unit to calculate from the public key,  $k_{pub}$  =  $h^{f(d)} \in H$ , element  $\pi(k_{pub}{}^{f(t)}) \in G$ , where  $\pi: H \to G$  specifies a mapping of the semigroup H into a group G,  $d \equiv k_{priv} \in T$  is the private key which is accessible only to the proving unit, and a mapping  $t \to h^{f(t)} \to \pi(h^{f(t)})$  from the subrange of the integers T to the group G represents a one-way function; and

using the verifying unit to encrypt the at least one data element, z, by a combination with respect to the encrypted data element,  $z' = z \circ \pi(k_{pub}{}^{f(t)}) \in G$ .

18. The method according to claim 17, which further comprises during the step d), in addition to the encrypted data element, using the verifying unit to communicate the element  $h^{f(t)} \in H$  to the proving unit.

19. The method according to claim 18, which further comprises performing the first cryptographic decryption method by the steps of:

using the proving unit to calculate the element  $k_{pub}^{f(t)} \in H$  using function f, the element  $h^{f(t)} \in H$  and the private key d known only to the proving unit;

using the proving unit to calculate an inverse element  $\pi'\left(k_{pub}{}^{f(t)}\right) \in G \text{ with respect to element } \pi(k_{pub}{}^{f(t)}) \in G; \text{ and }$ 

using the proving unit to decrypt the encrypted data element by a combination of the encrypted data element with inverse element:  $z=z'\circ\pi'(k_{pub}{}^{f(t)})$ , where the first cryptographic decryption method is based on the same mappings f,  $\pi$  and the same combination  $\circ$  as the first cryptographic encryption method.

20. The method according to claim 19, which further comprises performing the second cryptographic method with the steps of:

using the proving unit to calculate, from the at least one unencrypted data element z, an element  $g_2 = \pi_1(z) \in G_1$  and an element  $g_2 = \pi_2(z) \in G_2$ , where  $G_{-1}$  and  $G_2$  represent groups where

 $G_1 \subset G_2$  and  $\pi_1: G \to G_1$  and  $\pi_2: G \to G_2$  represent functions which map elements of the group G onto the groups  $G_1$  or  $G_2$ ;

using the proving unit to transform the data set to be authenticated m, to form an element  $g' = (g_1 * m)$  with a group combination \* in  $G_1$ ; and

using the proving unit to calculate the authenticator D, by D  $= \text{inj}(g') \bullet g_2 \text{ with the group combination} \bullet \text{ in } G_2, \text{ where the}$  mapping inj :  $G_1 \to G_2$  maps elements from  $G_1$  injectively into  $G_2$ .

21. The method according to claim 15, which further comprises performing the communication between the proving unit and the verifying unit contactlessly.